

$$15. \quad \frac{dx}{dt} = 2x + y + 3$$

$$\frac{dy}{dt} = -3x - 2y - 4$$

$$\begin{cases} 2x + y + 3 = 0 \\ -3x - 2y - 4 = 0 \end{cases}$$

$$\begin{cases} 2x + y + 3 = 0 \\ x = -\frac{2y+4}{3} \end{cases}$$

$$2 \cdot \left(-\frac{2y+4}{3}\right) + y + 3 = 0$$

$$-\frac{4y+8}{3} + \frac{3y}{3} + 3 = 0$$

$$-\frac{y+8}{3} = -3$$

$$-(y+8) = -9$$

$$-y - 8 = -9$$

$$y = 1$$

$$x = -\frac{2+4}{3} = -2$$

$$\text{ODP. : } (-2, 1)$$

$$16. \quad \frac{dx}{dt} = -5x + 2y$$

$$\frac{dy}{dt} = x - 4y$$

$$\begin{cases} -5x + 2y = 0 \\ x - 4y = 0 \end{cases}$$

$$\begin{cases} -5x + 2y = 0 \\ x = 4y \end{cases}$$

$$-5 \cdot 4y + 2y = 0$$

$$-20y + 2y = 0$$

$$y = 0$$

$$x = 0$$

$$\text{ODP. : } (0, 0)$$

$$17. \frac{dx}{dt} = 2x + 13y$$

$$\frac{dy}{dt} = -x - 2y$$

$$\begin{cases} 2x + 13y = 0 \\ -x - 2y = 0 \end{cases}$$

$$\begin{cases} 2x + 13y = 0 \\ x = -2y \end{cases}$$

$$2 \cdot (-2y) + 13y = 0$$

$$-4y + 13y = 0$$

$$y = 0$$

$$x = 0$$

$$\text{opp. : } (0, 0)$$

$$18. \frac{dx}{dt} = x(7 - x - 2y)$$

$$\frac{dy}{dt} = y(5 - x - y)$$

$$\begin{cases} x(7 - x - 2y) = 0 \\ y(5 - x - y) = 0 \end{cases}$$

$$\begin{cases} y = -\frac{x-7}{2} \\ y(5 - x - y) = 0 \end{cases}$$

$$-\frac{x-7}{2} (5 - x + \frac{x-7}{2}) = 0$$

$$-\frac{x-7}{2} = 0 \quad \vee \quad 5 - x + \frac{x-7}{2} = 0$$

$$x_1 = 7$$

$$y_1 = 0$$

$$\frac{10 - 2x + x - 7}{2} = 0$$

$$3 - x = 0$$

$$x_2 = 3$$

$$y_2 = -\frac{3-7}{2} = 2$$

$$\text{opp. : } (7, 0), (3, 2)$$